

$$\begin{aligned}
\sum_{i=1}^n \sum_{j=1}^n \frac{i^2 + j^2}{n^2} &= \frac{1}{n^4} \sum_{i=1}^n \sum_{j=1}^n (i^2 + j^2) \\
&= \frac{1}{n^4} \sum_{i=1}^n \left(\sum_{j=1}^n i^2 + \sum_{j=1}^n j^2 \right) \\
&= \frac{1}{n^4} \sum_{i=1}^n \left(n i^2 + \sum_{j=1}^n j^2 \right)
\end{aligned}$$